

Overview of typified DEB models & Tools

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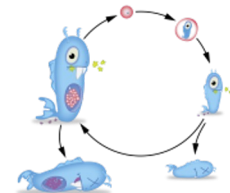
ΠΑΝΕΠΙΣΤΗΜΙΟ
ΚΡΗΤΗΣ

UNIVERSITY
OF CRETE



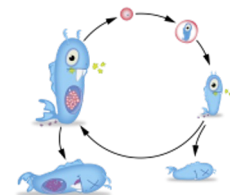
MARETEC
MARINE, ENVIRONMENT
AND TECHNOLOGY CENTER
TÉCNICO LISBOA

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deb2023.sciencesconf.org



Lecture outline

- Overview of the standard DEB model
- Types of DEB parameters
- Deviations from the standard DEB model
- Extensions of DEB models
- AmP tool for simulating and plotting trajectories of the state of an individual and some traits in constant and dynamic environment (food/temperature)



Standard (std) DEB model

1 food type, 1 reserve, 1 structure, isomorph,
reproduces by means of eggs

Dynamics of the state variables

$$\frac{dV}{dt} = \frac{\dot{p}_G}{[E_G]}$$

$$\frac{dE}{dt} = \dot{p}_A - \dot{p}_C$$

$$\frac{dE_H}{dt} = \dot{p}_R(E_H < E_H^p)$$

$$\frac{dE_R}{dt} = \kappa_R \dot{p}_R(E_H \geq E_H^p)$$

$$\dot{p}_A = (E_H \geq E_H^b) \{ \dot{p}_{Am} \} f(X) V^{2/3}$$

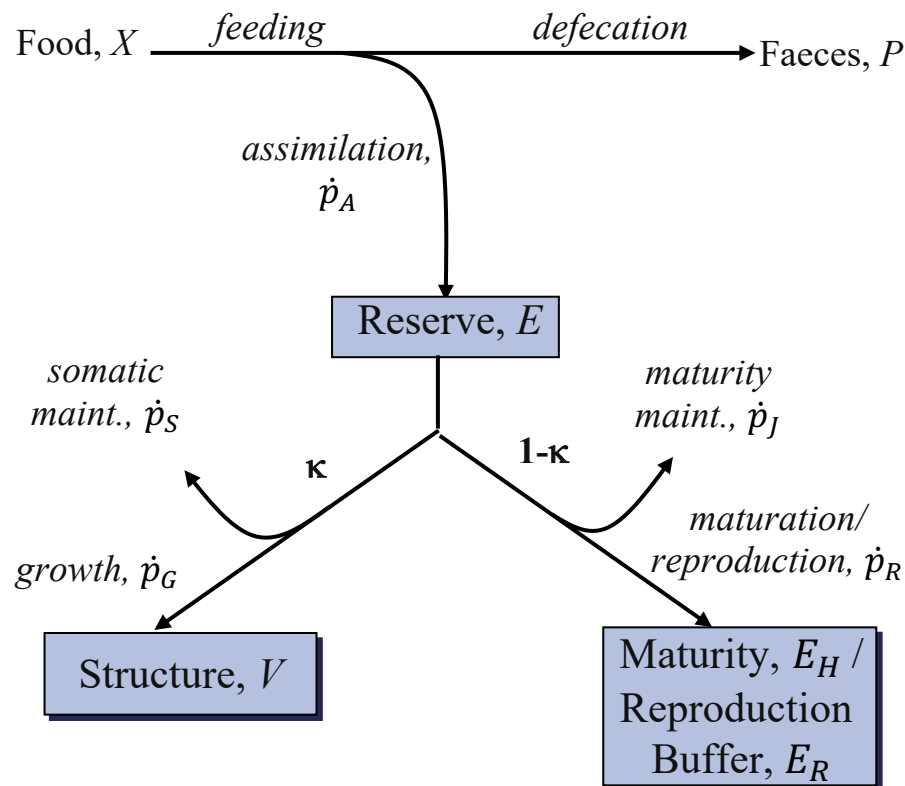
$$\dot{p}_C = E \frac{[E_G] \dot{v}/L + [\dot{p}_S]}{\kappa[E] + [E_G]}$$

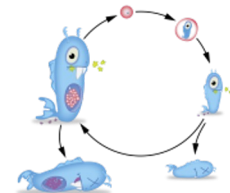
$$\dot{p}_G = \kappa \dot{p}_C - \dot{p}_S$$

$$\dot{p}_S = [\dot{p}_M]V + \{ \dot{p}_T \} V^{2/3}$$

$$\dot{p}_J = \dot{k}_J E_H$$

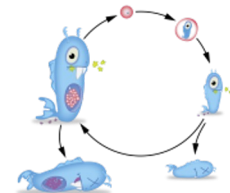
$$\dot{p}_R = (1 - \kappa) \dot{p}_C - \dot{p}_J$$





Type of DEB parameters

- **Core parameters**
 - Control changes of the state variables
 - Linked to the concepts on which the model is based
- **Auxiliary parameters**
 - Convert measurements (e.g., from dry to wet mass, length to volume etc.)
 - Quantify effects of temperature on rates and time
- **Primary parameters**
 - Connected to a single underlying process
- **Compound parameters**
 - Depend on several underlying processes
 - Functions of other parameters



Primary parameters

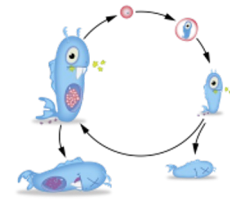
assimilation	$\{\dot{p}_{Am}\}$	max surface-specific assim rate ($\text{J cm}^{-2} \text{ d}^{-1}$)
feeding	$\{\dot{F}_m\}$	surface- specific searching rate ($\text{l d}^{-1} \text{ cm}^{-2}$)
digestion	κ_X	digestion efficiency (-)
mobilisation	$\dot{v}$	energy conductance (cm d^{-1})
allocation	κ	allocation fraction to soma (-)
reproduction	κ_R	reproduction efficiency (-)
turnover, activity	$[\dot{p}_M]$	volume-spec. som. maint. costs ($\text{d}^{-1}\text{cm}^{-3}$)
heating, osmosis	$\{\dot{p}_T\}$	surface-spec. som. maint. costs ($\text{d}^{-1}\text{cm}^{-2}$)
development	$\dot{k}_J$	maturity maint. rate coefficient (d^{-1})
growth	$[E_G]$	specific growth for structure (J cm^{-3})
life cycle	E_H^b	maturity at birth (J)
life cycle	E_H^p	maturity at puberty (J)
aging	$\dot{h}_a$	Weibul aging acceleration (d^{-2})
aging	s_G	Gompertz stress coefficient (-)

Examples of compound parameters

$$[E_m] = \frac{\{\dot{p}_{Am}\}}{\dot{v}} \quad \text{max reserve density}$$

$$L_m = \frac{\kappa\{\dot{p}_{Am}\}}{[\dot{p}_M]} \quad \text{max structural length}$$

Auxiliary parameters



Conversion parameters

δ_M	shape coefficient (-)
$d_O = (d_X d_V d_E d_P)$	specific densities (g/cm ³)
$\mu_O = (\mu_X \mu_V \mu_E \mu_P)$	chemical potentials (organics) (J/mol)
$\mu_M = (\mu_C \mu_H \mu_O \mu_N)$	chemical potentials (minerals) (J/mol)
$n_O = (n_X n_V n_E n_P)$	chemical indices (organics) (-)
$n_M = (n_C n_H n_O n_N)$	chemical indices (minerals) (-)
$w_O = (12 \ 1 \ 16 \ 14)$	molecular weights (g/mol)

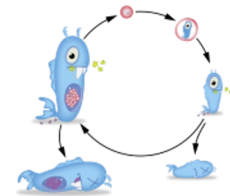
<i>O</i>	organics
<i>M</i>	minerals
<i>X</i>	food
<i>V</i>	structure
<i>E</i>	reserve
<i>P</i>	faeces
<i>C</i>	CO ₂
<i>H</i>	H ₂ O
<i>O</i>	O ₂
<i>N</i>	N-waste

Temperature parameters

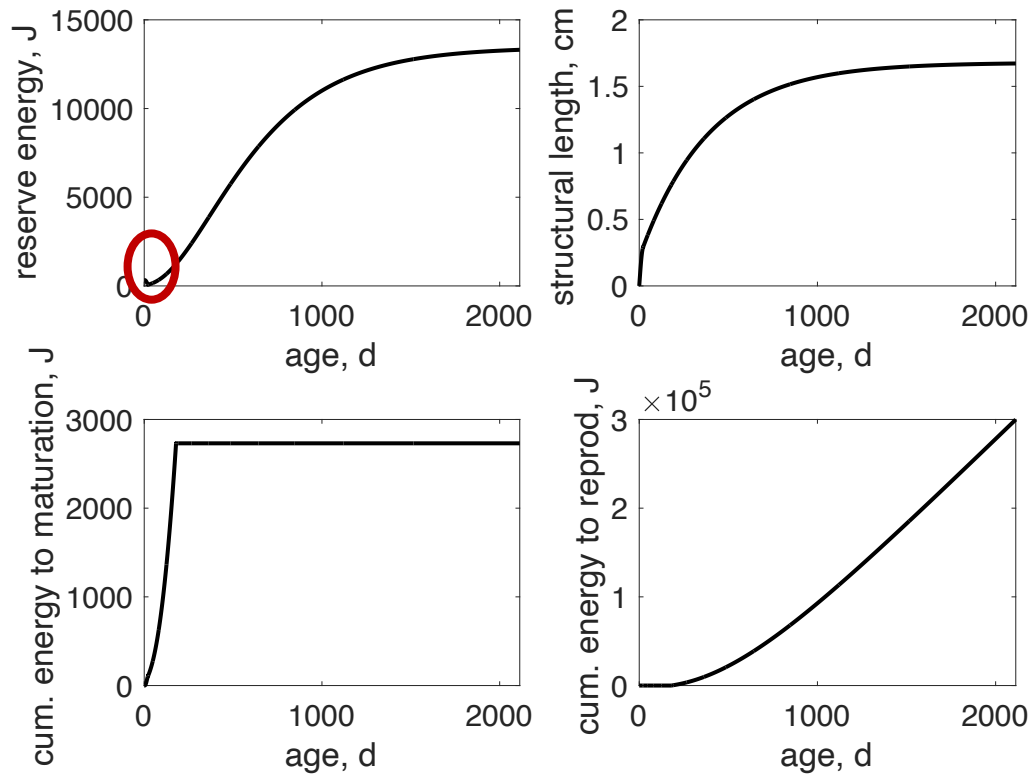
T_{ref}	reference temperature (273 K)
T_A	Arrhenius temperature
T_L, T_H	temperature tolerance range
T_{AL}, T_{AH}	Arrhenius temperatures for transitions to inert state

Individual Dynamics

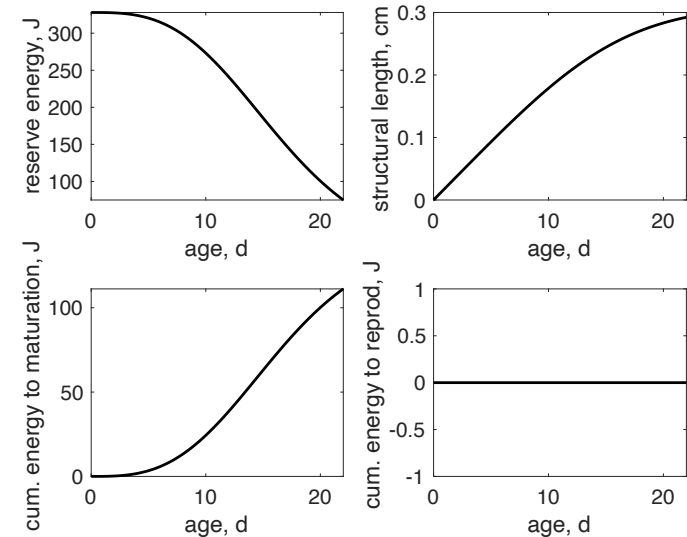
from start of development to death by aging



Constant environment

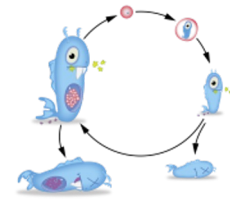


Embryo dynamics

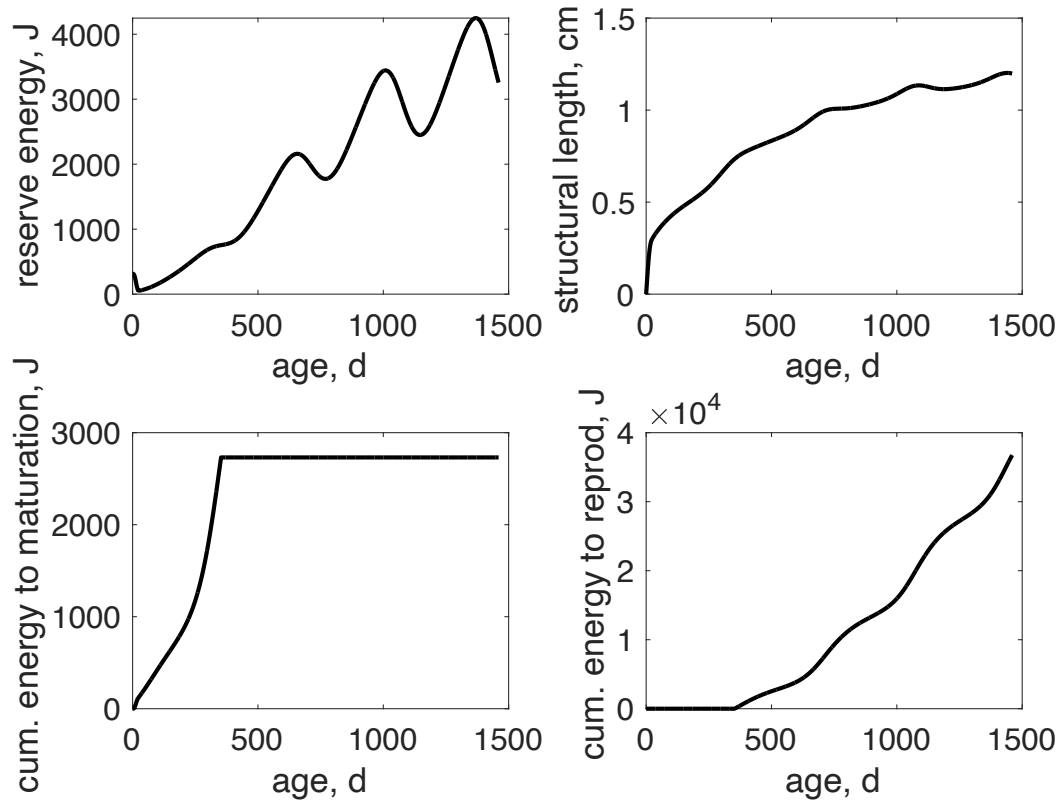


Hippocampus whitei (White's seahorse)

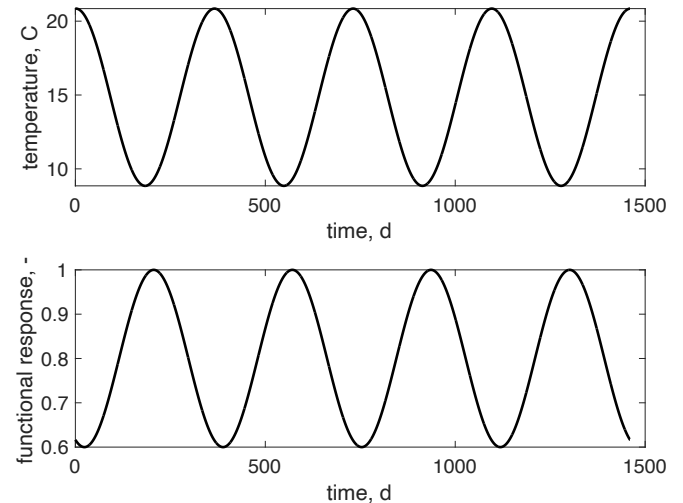
Individual Dynamics



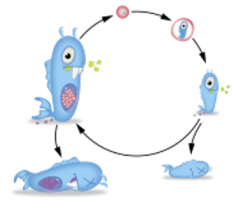
Varying environment



Temp and food variation



Life Stages



Morphological life stages

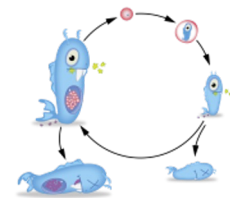
refer to the physical or structural changes that an organism undergoes throughout its life cycle. E.g., egg, larva, pupa, and imago in insects
tadpole and frog in amphibians

Functional life stages

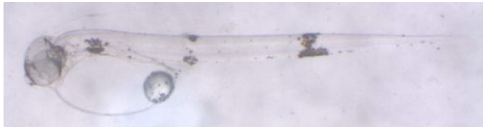
refer to functional or physiological changes that occur during the life cycle of an organism. E.g. embryo, juvenile, adults



Deviations from the std DEB model



European sea bass, *Dicentrarchus labrax*



15dph



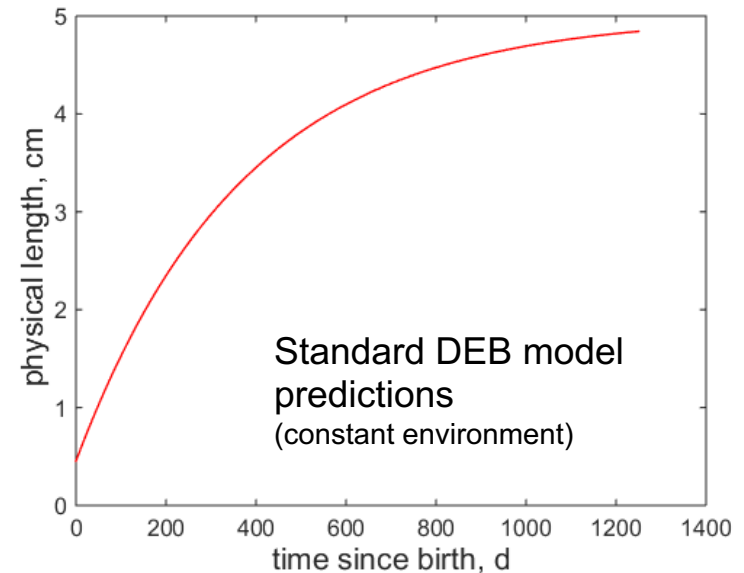
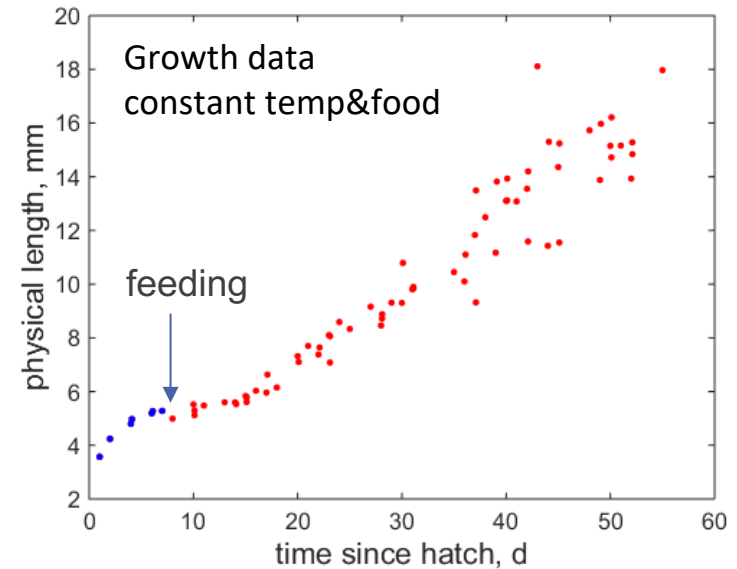
35 dph (fins)



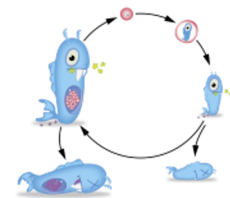
juvenile

juvenile

Life stages: egg, larvae, juvenile, adult



Deviations from the std DEB model

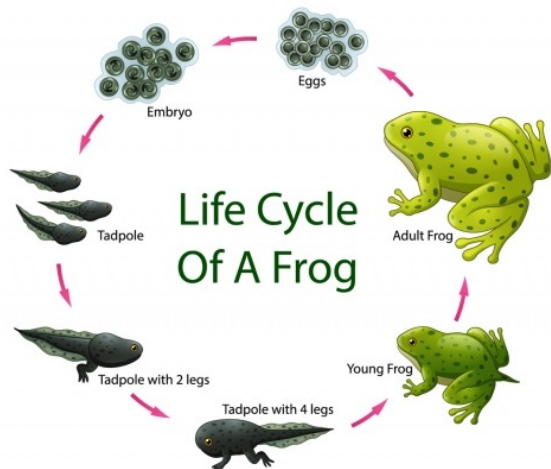


Fetal development



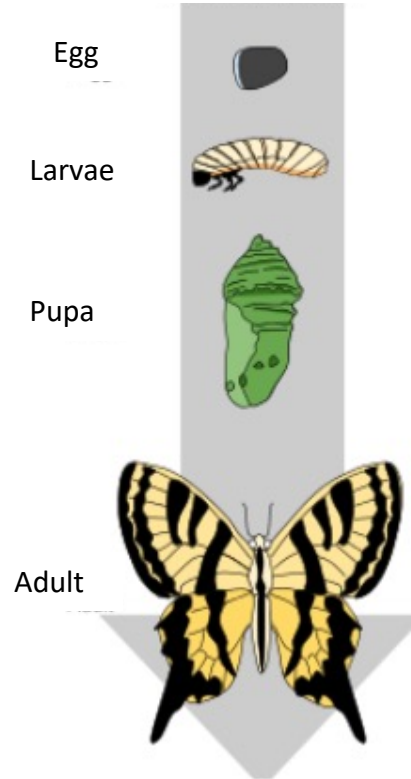
Koala
Phascolarctos cinereus
Author: Bas Kooijman

Changes in morphology

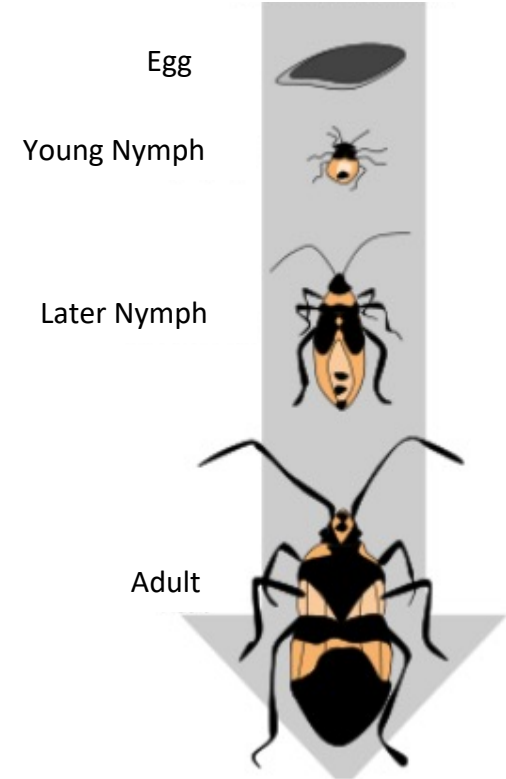


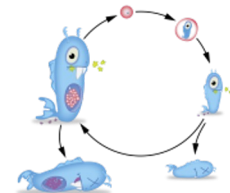
(Source: [Dualororua](#))

Holometabolous



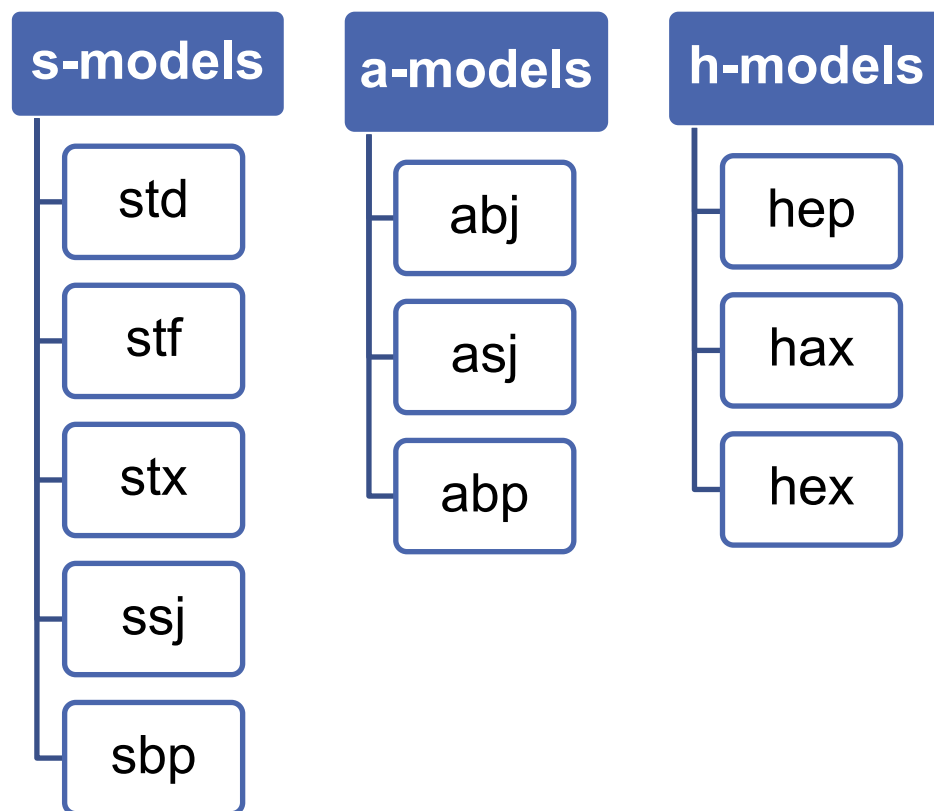
Hemimetabolous



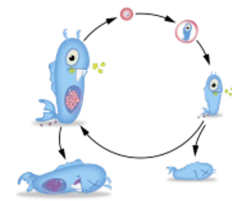


Typified Models in AmP

- To accommodate complex life-cycles, various forms of metabolic acceleration and fetal development different models of DEB theory have been applied to different organisms.
- All are related and consistent with the DEB theory.
- They are extensions of the standard DEB model.
- For the purpose of standardizing parameter estimation some extensions of the standard DEB model have been formalized and are called “typified” models.



s-models



Assume isomorphy throughout the full life cycle: **surface area $\propto$ volume^{2/3}**

s-models	Description	%entries in AmP
std	standard DEB model with egg development	49.12%
stf	std with foetal development	1.24%
stx	stf with baby stage until weaning x ($b < x < p$)	17.70%
ssj	std with non-feeding stage between s and j ($b < s < j < p$)	0.20%
sbp	std with growth ceasing at puberty	0.07%



Squalus acantias
std



Monachus monachus
stx



Oedura_monilis
stf



Oedura_monilis
ssj

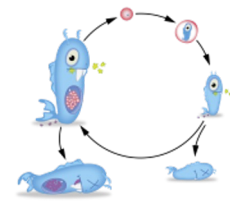


Phascolarctos cinereus
stx



Tigriopus brevicornis
sbp

a-models



Assume isomorphy, but during part of the life cycle metabolism accelerates following the rules for V1-morphy **surface area $\propto$ volume**

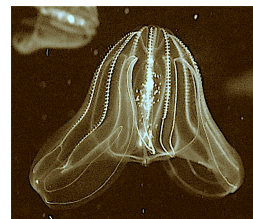
a-models	Description	%entries in AmP
abj	std with acceleration between birth b and metamorphosis j ($b < j < p$)	31.71%
asj	abj with delayed acceleration starting at s ($b < s < j < p$)	0.10%
abp	abj with growth ceasing at puberty	0.30%



Dicentrarchus labrax
abj



Mytilus edulis
abj



Mnemiopsis leidyi
asj

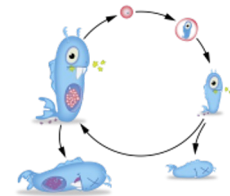


Eurytemora affinis
abp



Locusta migratoria
abp

M acceleration: modelled with a-models

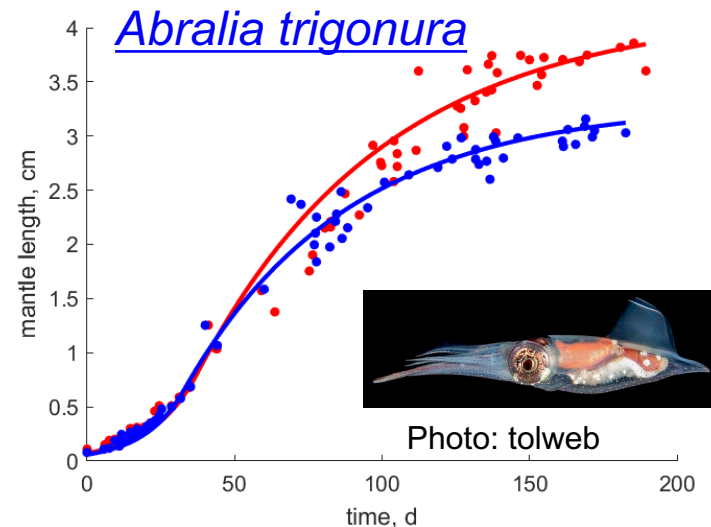


M-type acceleration is observed in most invertebrate species with morphological metamorphosis, but also to some taxa without.

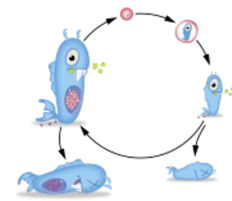
Recognize M acceleration by upcurving of length-at-age at constant food and temperature.

Surface area proportional to volume during M acceleration. This affects both specific assimilation $\{\dot{p}_{Am}\}$ and energy conductance $\dot{v}$, which increase with length.

The end of acceleration is controlled by the maturity level passing a threshold value.



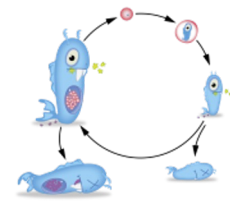
h-models



h-models are as a-models, but with extra life stages

h-models	Description	%entries in AmP
hep		0.17%
hex		0.25%
hax		0.15%

AmP tool for simulating and plotting individual dynamics



Work in progress

Available for the std and sbp models
and all a-models

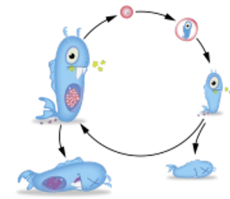
species: species_name
tT: time-temperature
tf: time-functional response

<https://amptool.debtheory.org/docs/index.html>

simu_my_pet.m
calls
get_indDyn_mod.m

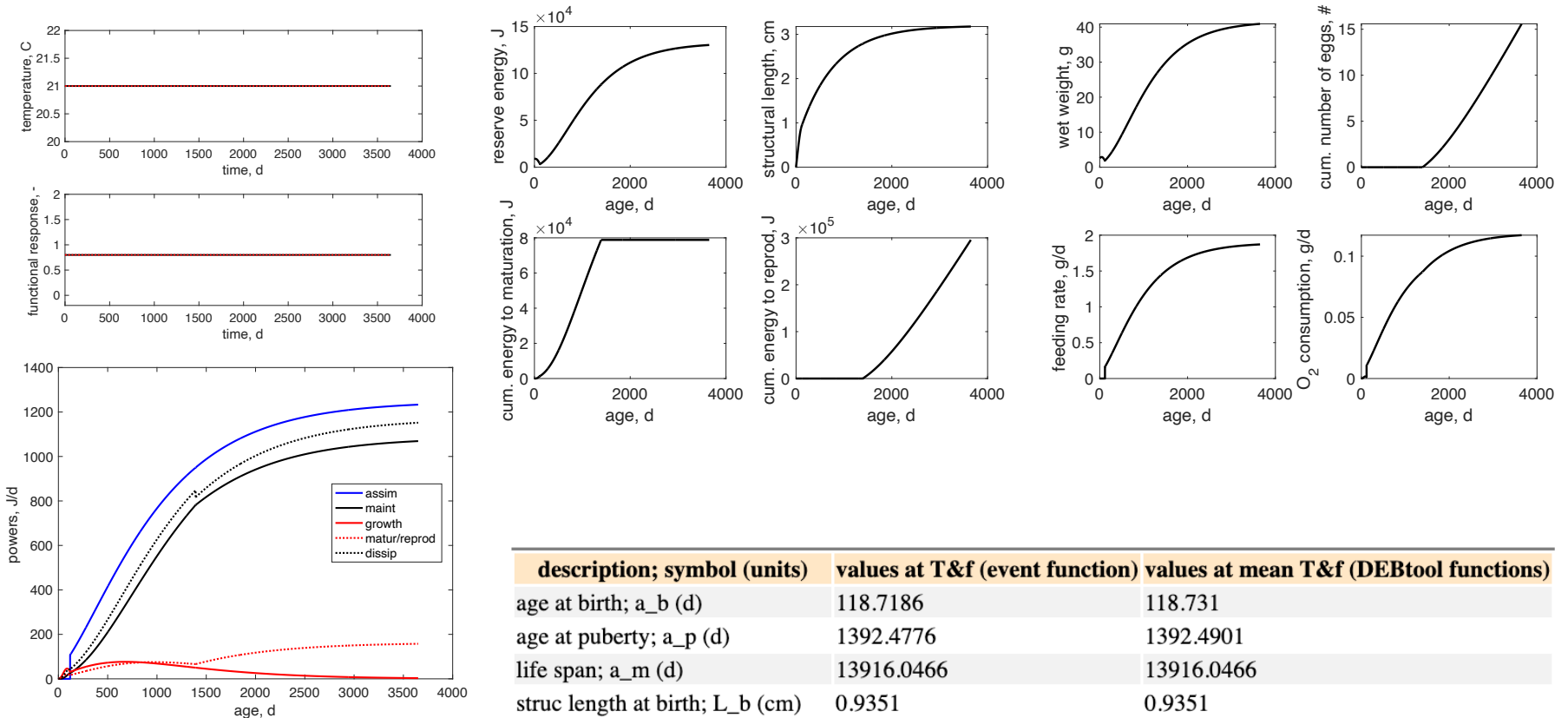
Plots: Environmental variables
State variables: E , L , E_H , E_R
Observable quantities: weight, fecundity, feeding, O2 consumption
Powers
Table with age, weight at life events

Megalobulimus mogianensis (snail)

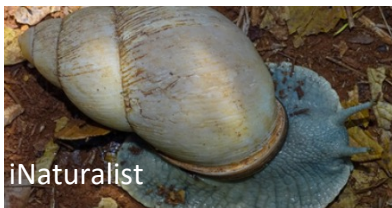


```
simu_my_pet('Megalobulimus_mogianensis', C2K(21),0.8)
```

```
simu_my_pet('Megalobulimus_mogianensis', [0 C2K(21); 10*365 C2K(21)] ,0.8)
```

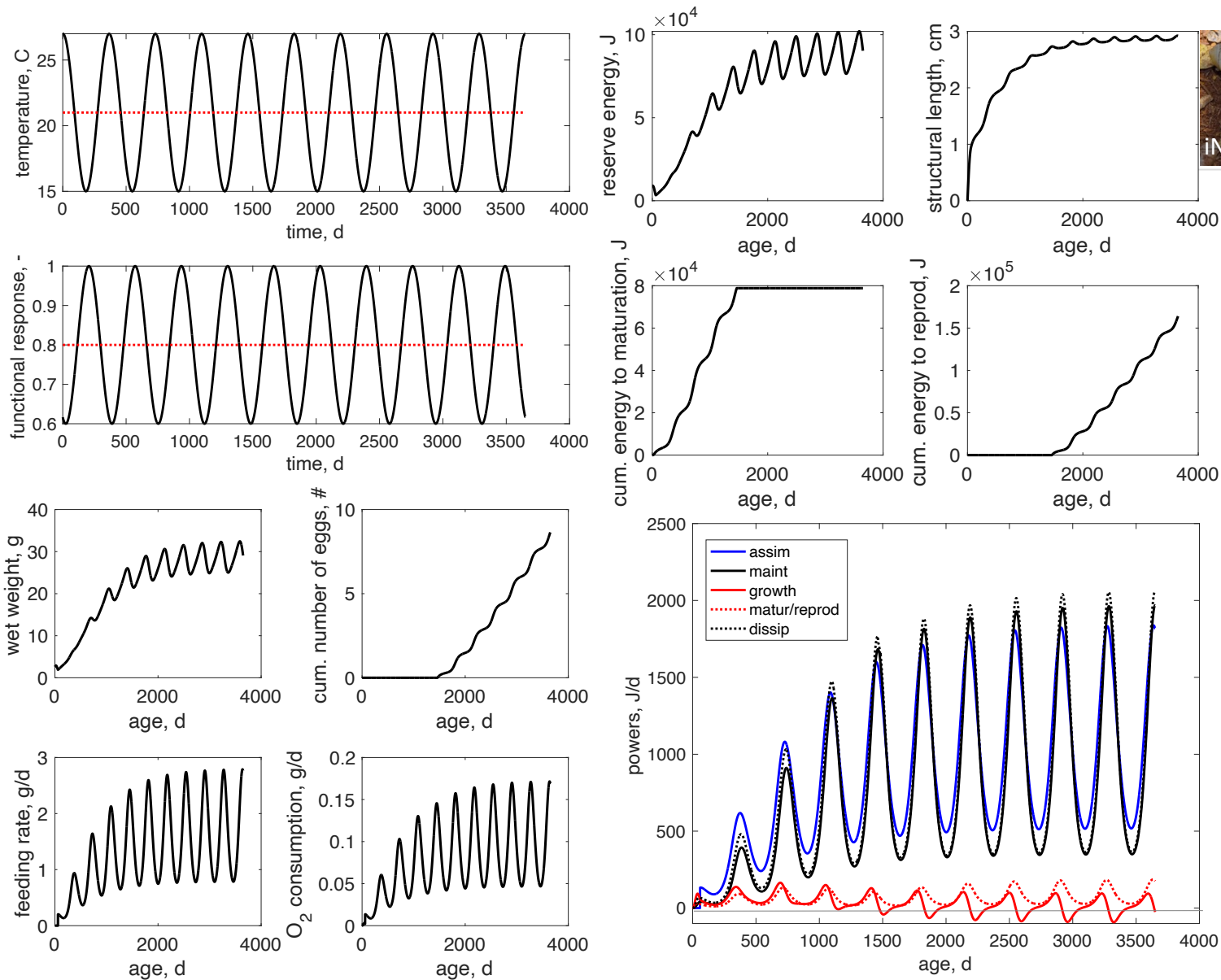
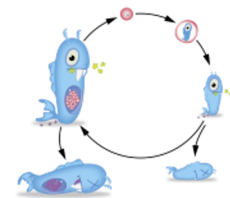


description; symbol (units)	values at T&f (event function)	values at mean T&f (DEBtool functions)
age at birth; a_b (d)	118.7186	118.731
age at puberty; a_p (d)	1392.4776	1392.4901
life span; a_m (d)	13916.0466	13916.0466
struc length at birth; L_b (cm)	0.9351	0.9351
struc length at puberty; L_p (cm)	2.7888	2.7888
ultimate length; L_i (cm)	NaN	3.1967
wet weight at birth; Ww_b (g)	1.7803	1.7803
wet weight at puberty; Ww_p (g)	47.2259	47.2259
ultimate wet weigh; Ww_i (g)	NaN	71.1273

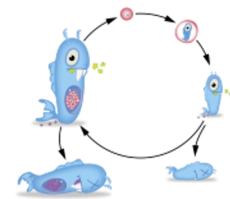


iNaturalist

Megalobulimus mogianensis (snail)



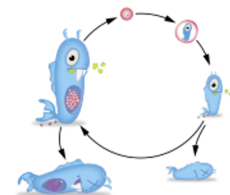
Megalobulimus mogianensis (snail)



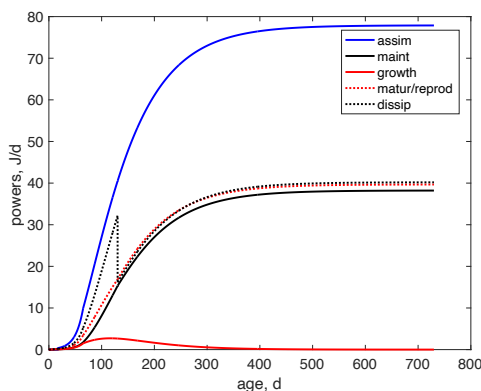
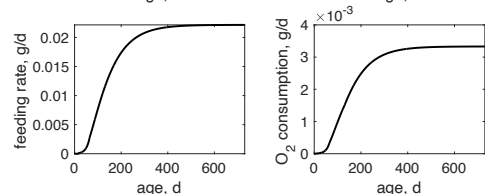
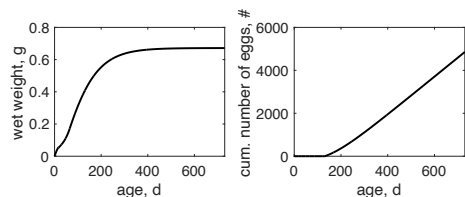
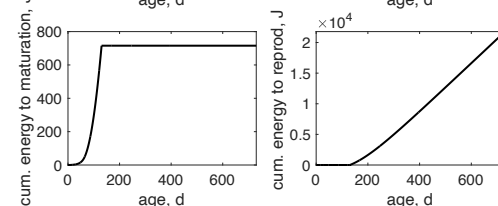
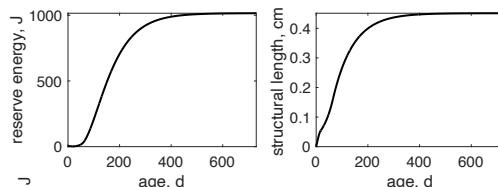
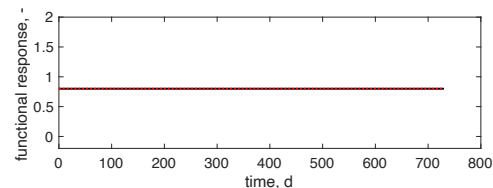
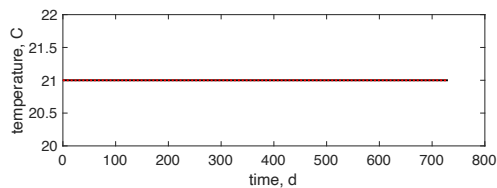
description; symbol (units)	values at T&f (event function)	values at mean T&f (DEBtool functions)
age at birth; a_b (d)	59.0791	101.4495
age at puberty; a_p (d)	1462.846	1189.9145
life span; a_m (d)	13913.7321	13913.7321
struc length at birth; L_b (cm)	0.9351	0.9351
struc length at puberty; L_p (cm)	2.7312	2.7888
ultimate length; L_i (cm)	NaN	3.1966
wet weight at birth; Ww_b (g)	1.7803	1.7803
wet weight at puberty; Ww_p (g)	41.4613	47.2229
ultimate wet weigh; Ww_i (g)	NaN	71.1158

Examples of variable T and f

```
t = linspace(0, 10*365, 5000); tT_0 = 90; tf_0 = 250;  
T = C2K(21) + 6 * sin(2 * pi * (t + tT_0)/ 365);  
f = 0.8 + 0.2 * sin(2 * pi * (t + tf_0)/365);  
tT =[t',T']; tf =[t',f'];  
simu_my_pet('Megalobulimus_mogianensis', tT ,tf)
```



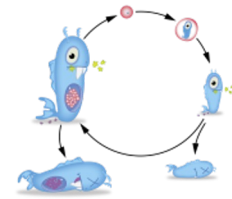
Oryzias latipes (medaka)



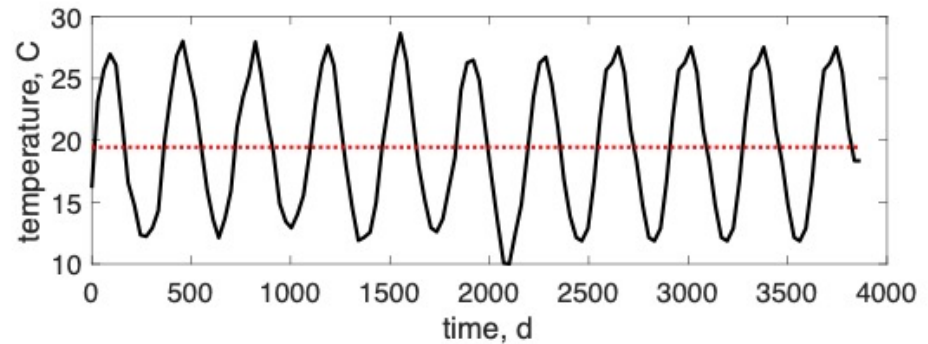
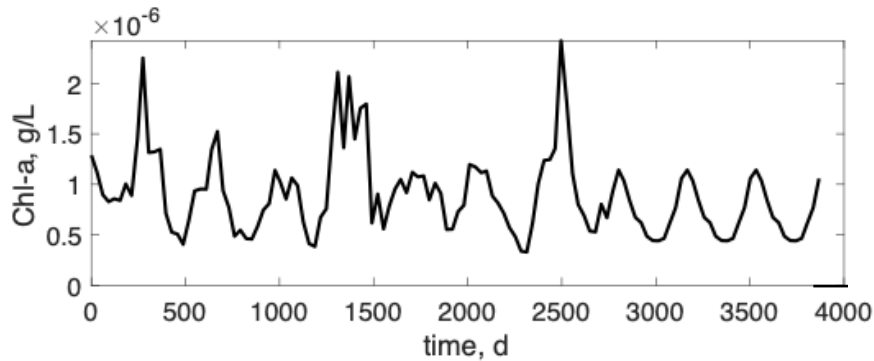
```
simu_my_pet('Oryzias_latipes', [0 C2K(21);  
2*365 C2K(21)] ,0.8)
```

description; symbol (units)	values at T&f (event function)	values at mean T&f (DEBtool functions)
age at birth; a_b (d)	17.3779	17.4055
age at metamorphosis; a_j (d)	64.9835	65.0133
age at puberty; a_p (d)	130.2999	130.3334
life span; a_m (d)	325.5821	325.5821
struc length at birth; L_b (cm)	0.053987	0.053989
struc length at metamorphosis; L_j (cm)	0.1612	0.1612
struc length at puberty; L_p (cm)	0.32525	0.32525
ultimate length; L_i (cm)	NaN	0.45104
wet weight at birth; Ww_b (g)	0.00053595	0.00053588
wet weight at metamorphosis; Ww_j (g)	0.014264	0.014264
wet weight at puberty; Ww_p (g)	0.11717	0.11717
ultimate wet weigh; Ww_i (g)	NaN	0.31247

Pinna nobilis (Noble pen shell)

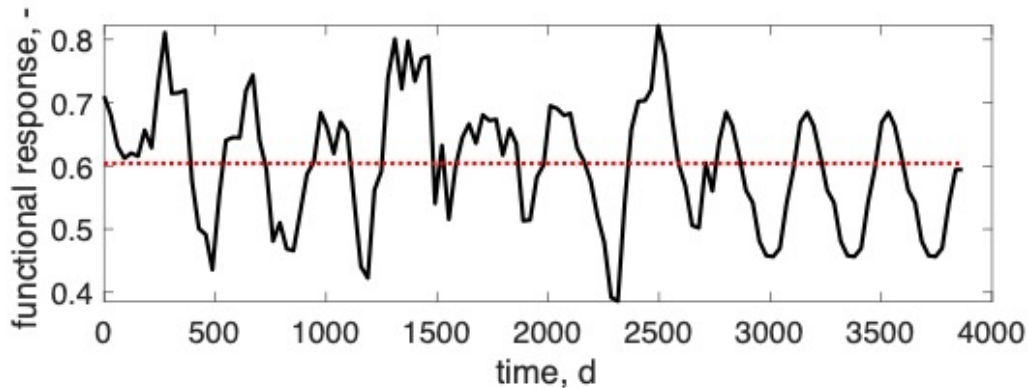


Temperature and Chl-a data from the Thermaic gulf in Greece

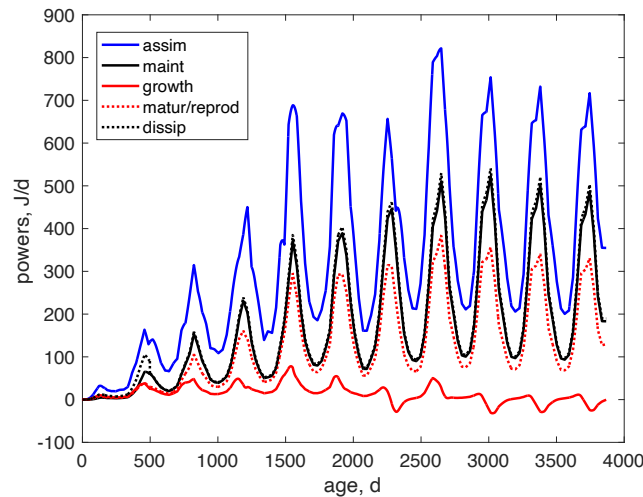
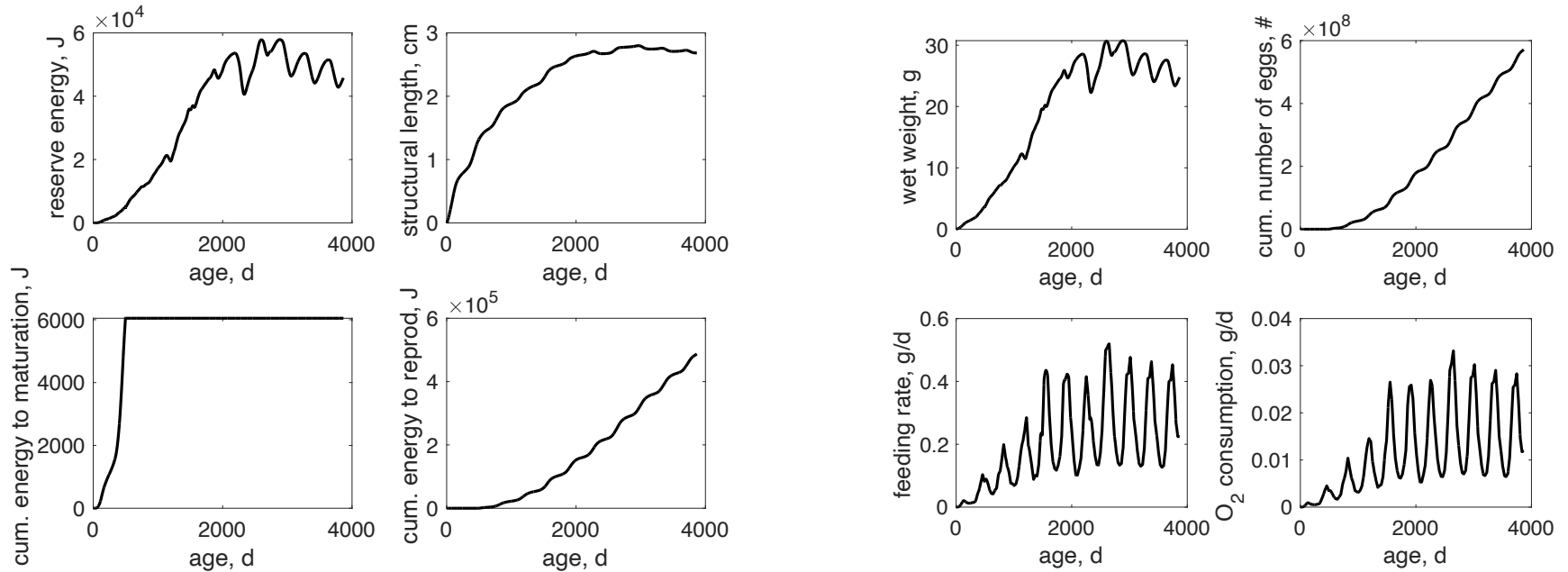
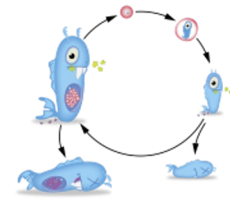


$$f = \frac{X}{K + X}$$

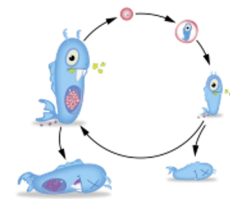
Half saturation constant
 $K = 5.25 \times 10^{-7}$ g/L



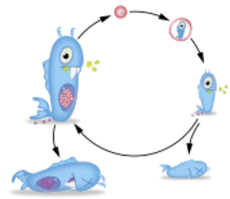
Pinna nobilis (Noble pen shell)



Pinna nobilis (Noble pen shell)



description; symbol (units)	values at T&f (event function)	values at mean T&f (DEBtool functions)
age at birth; a_b (d)	3.3825	2.2186
age at metamorphosis; a_j (d)	9.3609	7.0539
age at puberty; a_p (d)	497.9067	560.4616
life span; a_m (d)	3583.4854	3583.4854
struc length at birth; L_b (cm)	0.0048664	0.0048664
struc length at metamorphosis; L_j (cm)	0.014084	0.014083
struc length at puberty; L_p (cm)	1.3181	1.3275
ultimate length; L_i (cm)	NaN	3.0907
wet weight at birth; Ww_b (g)	2.6769e-07	2.6769e-07
wet weight at metamorphosis; Ww_j (g)	7.0892e-06	6.4876e-06
wet weight at puberty; Ww_p (g)	4.6704	5.4336
ultimate wet weigh; Ww_i (g)	NaN	68.5765



Thank you for your attention!!!

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